

# Bayes, not Naïve

Security Bounds on Website Fingerprinting Defenses

Giovanni Cherubin

Privacy Enhancing Technologies Symposium

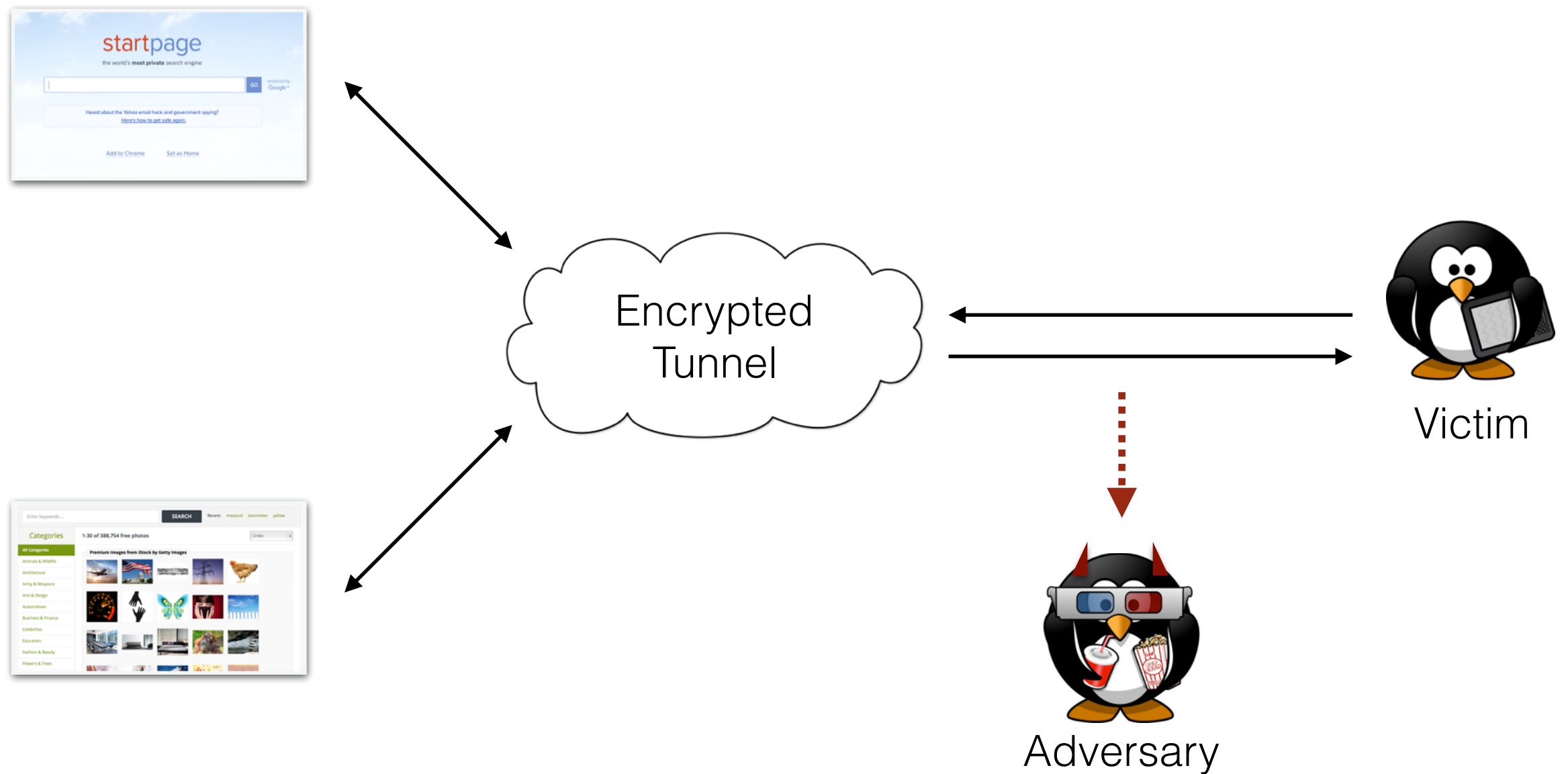
Minneapolis, Minnesota, USA

19 July, 2017

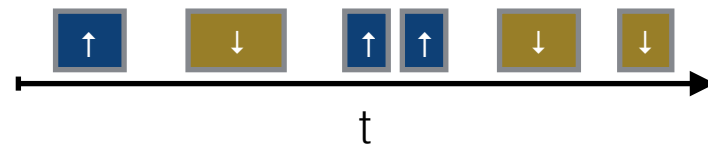
@gchers



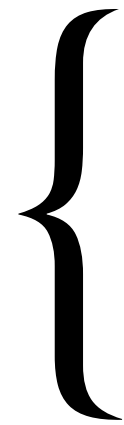
# Website Fingerprinting (WF)



# Website Fingerprinting (WF)



Adversary



$\Phi$ : transmission time,  
total bandwidth, ...

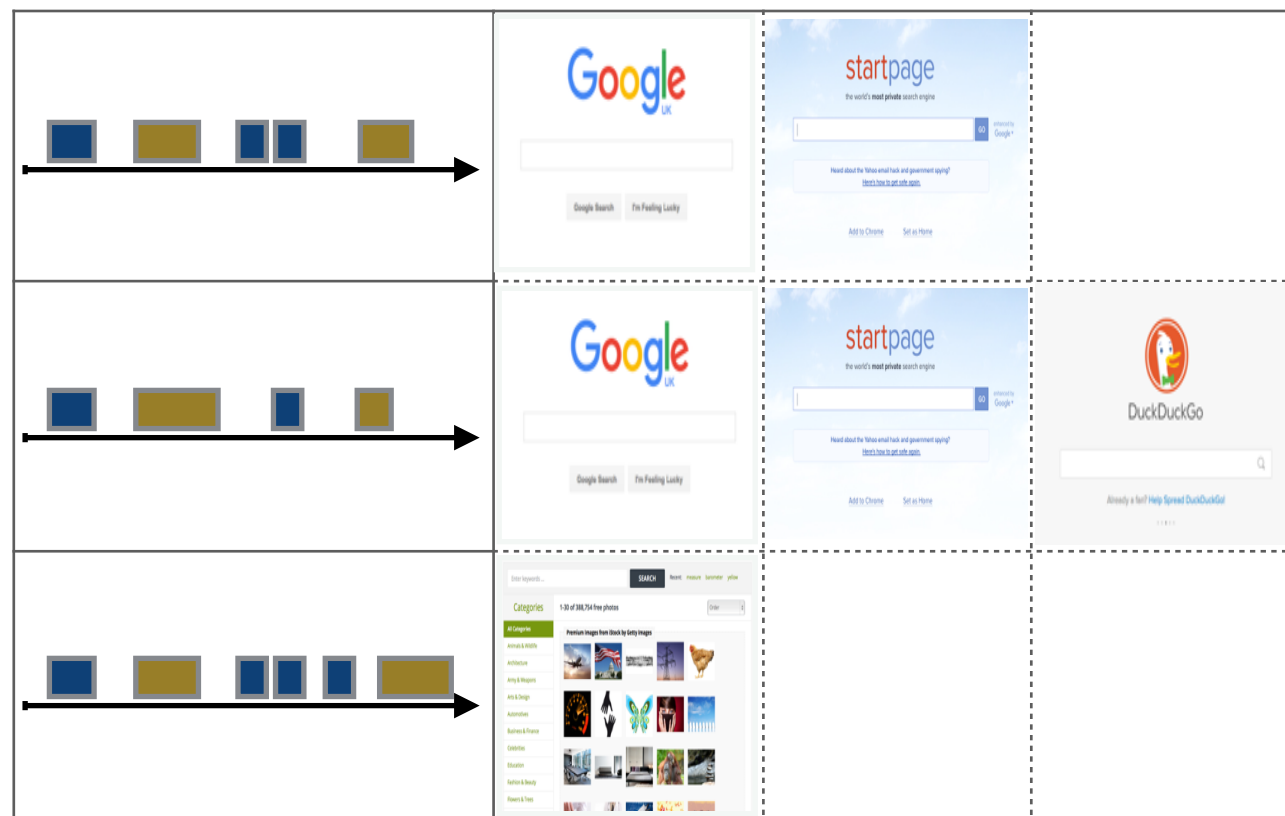
$f_{\text{train}}$ : SVM, logistic  
regression, ...

# “Lookup-Table” Approach

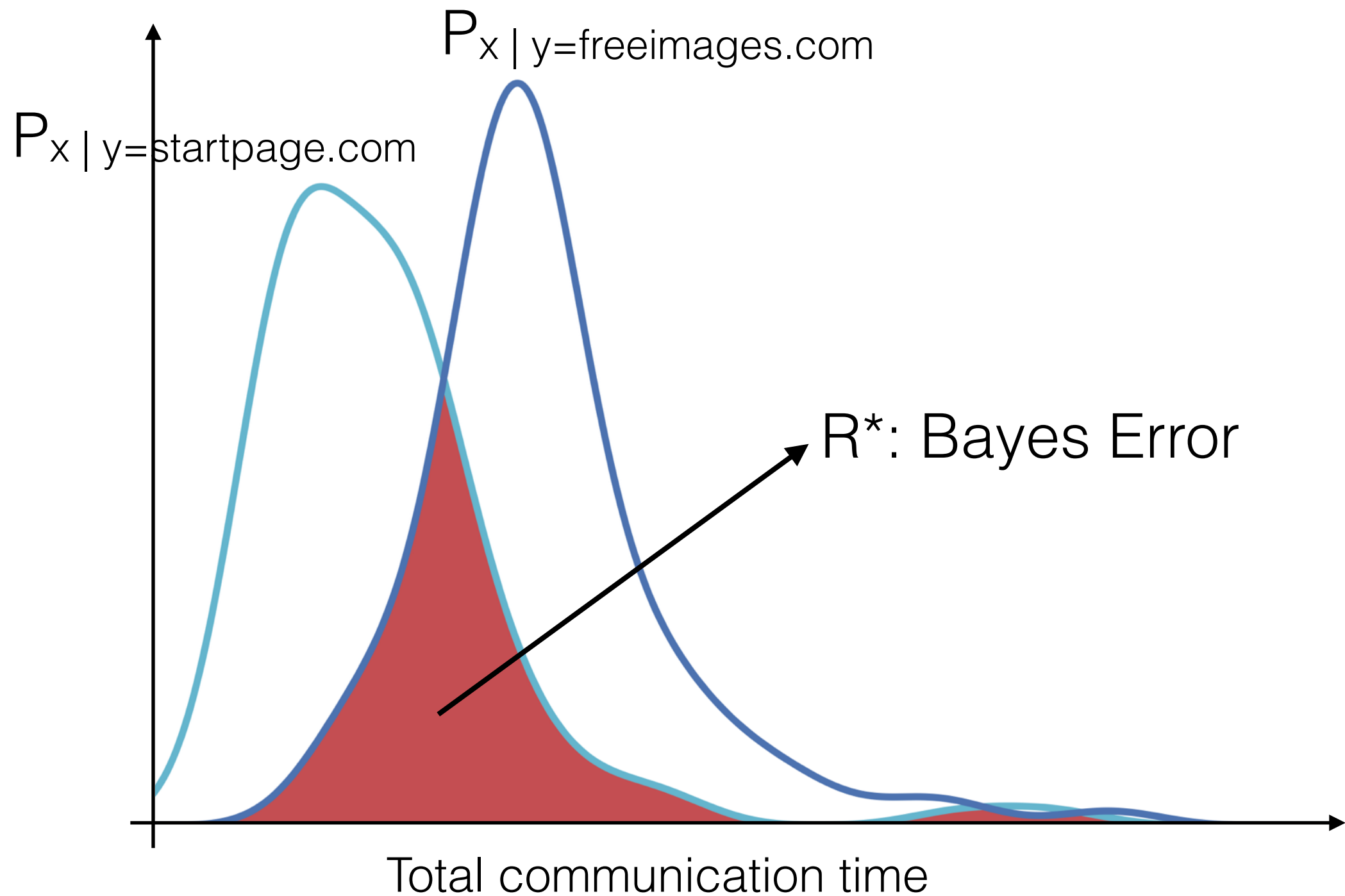
(Cai et al., '14)

Idealised Adversary: knows exactly what packet sequences each web page may generate. Count the collisions.

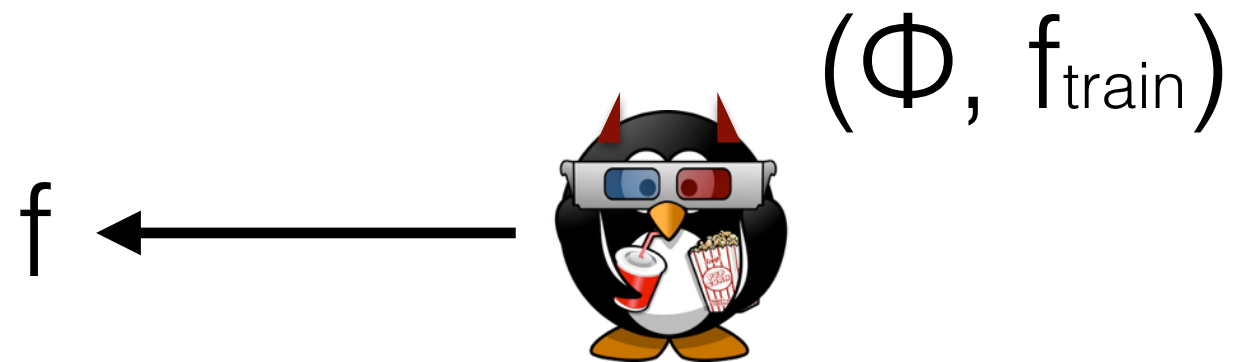
Lookup table



# Distinguishing Web Pages



# “Bayes estimate” approach



$R^f$  : error on new packet sequence

$$\frac{L-1}{L} \left( 1 - \sqrt{1 - \frac{L}{L-1} R^{NN}} \right) \leq R^* \leq R^f$$

(Cover & Hart, '67)

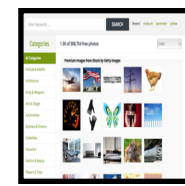
# $(\epsilon, \Phi)$ -privacy

**Problem** An error estimate  $\hat{R}^*$  alone does not convey information about the setting. Random guessing  $R^G$ :



?

$$R^G = 2/3$$



?

$$R^G = 1/2$$

Define metric  $(1 - Adv)$ :

$$\epsilon = \hat{R}^* / R^G$$

# $(\epsilon, \Phi)$ -privacy

Closed World, WCN+ dataset (Tor traffic)

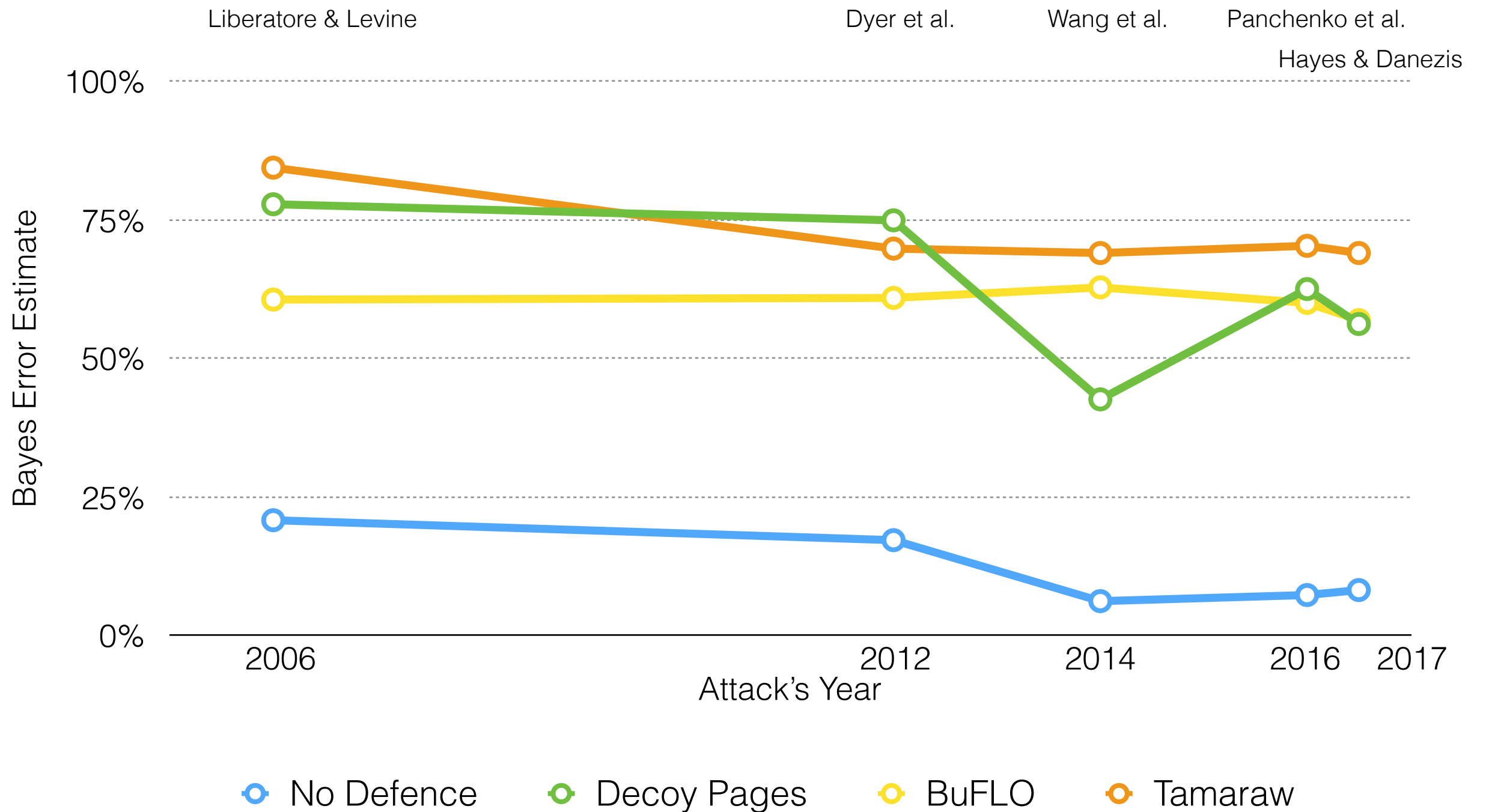
<b>Defense*</b>	<b><math>(\epsilon, \Phi)</math>-privacy</b>	<b>Packet OH</b>	<b>Time OH</b>
<b>No Defence</b>	(0.06, k-NN)	0%	0%
<b>Decoy Pages</b>	(0.43, k-NN)	134%	59%
<b>WTF-PAD</b>	(0.49, k-FP)	247%	0%
<b>BuFLO</b>	(0.58, k-FP)	110%	79%
<b>CS-BuFLO</b>	(0.63, k-FP)	67%	576%
<b>Tamaraw</b>	(0.70, k-NN)	258%	341%

\* Tor's default defense, Randomized Pipelining, is underlying each defense



(How much)

# Did Feature Sets Improve?



# Summary & Future Work

Blackbox method to derive security bounds for any WF defense and adversary  $(\Phi, \cdot)$

## **Future Work**

- Prove some  $\Phi$  is complete in some sense (“efficient”): from  $(\epsilon, \Phi)$ -privacy to  $\epsilon$ -privacy
- Other estimates of  $R^*$ , ensembles
- Other applications of technique: traffic analysis, side channel, generic ML-based attacks

# Bayes, not Naïve

Security Bounds on Website Fingerprinting Defenses

Giovanni Cherubin

Privacy Enhancing Technologies Symposium

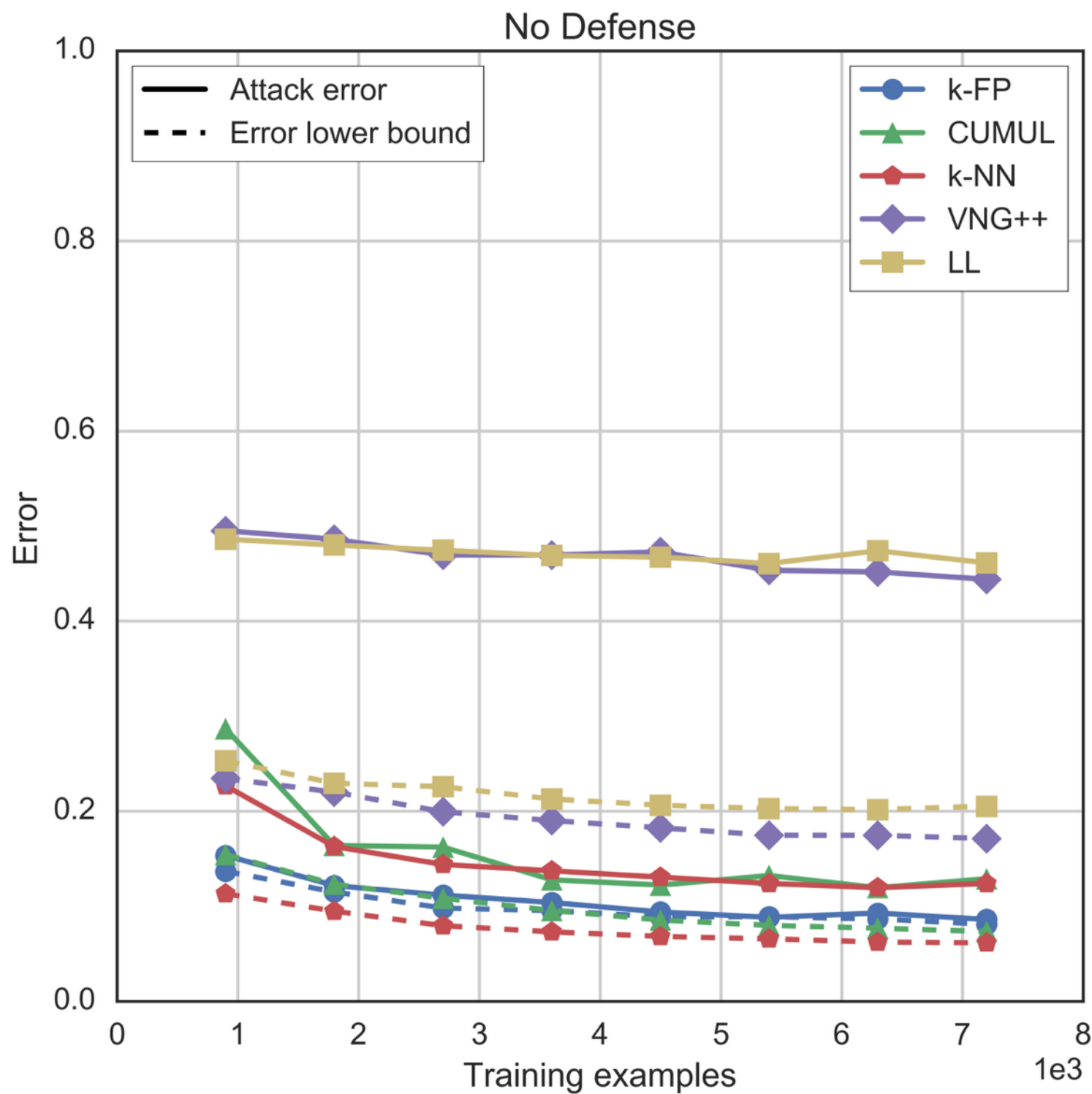
Minneapolis, Minnesota, USA

19 July, 2017

@gchers



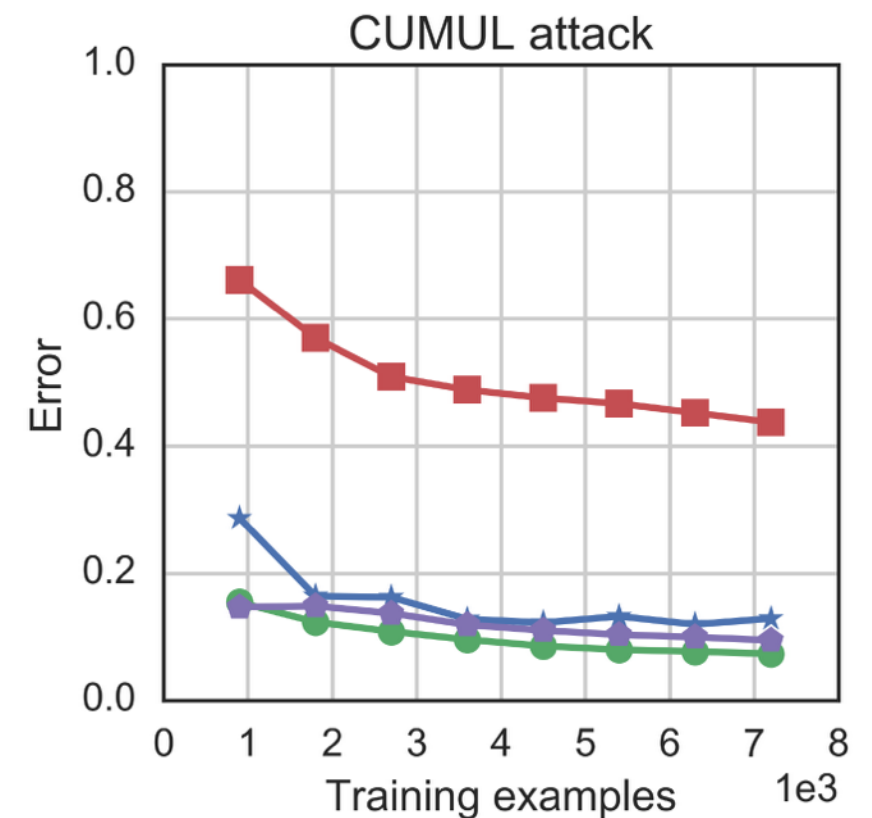
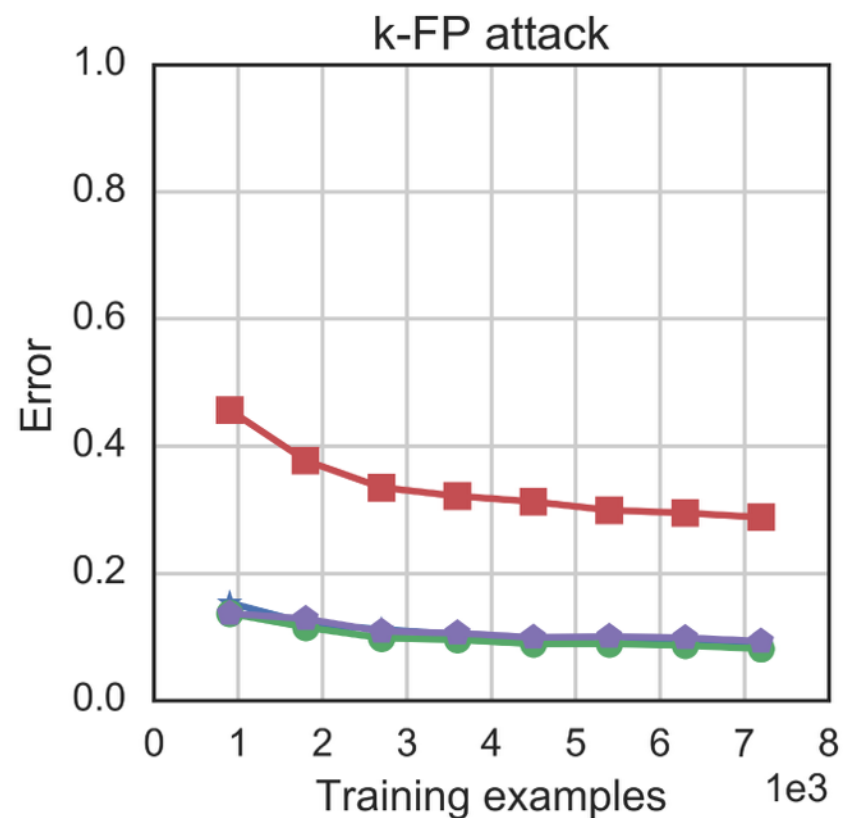
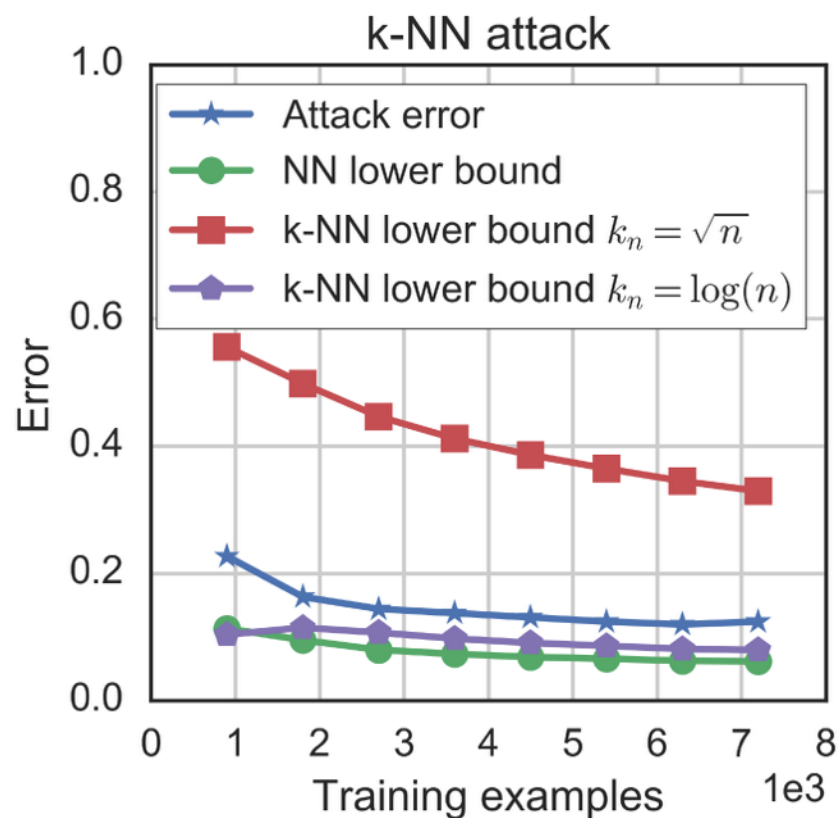
# Lower bound convergence



# k-NN Bayes Estimate

(Stone, '77)

**Theorem** Let  $k_n \rightarrow \infty$  and  $k_n/n \rightarrow 0$  as  $n \rightarrow \infty$ , then  
 $R^{k\text{-NN}} \rightarrow R^*$



# Comparison with Cai et al.

<b>Defence</b>	<b>R* estimate</b>	<b>Cai et al.</b>	<b>Cai et al. (full information)</b>
<b>BuFLO</b>	57%	53%	19%
<b>Tamaraw</b>	69%	91%	11%

# $(\epsilon, \Phi)$ -privacy

One VS All scenario, WCN+ dataset

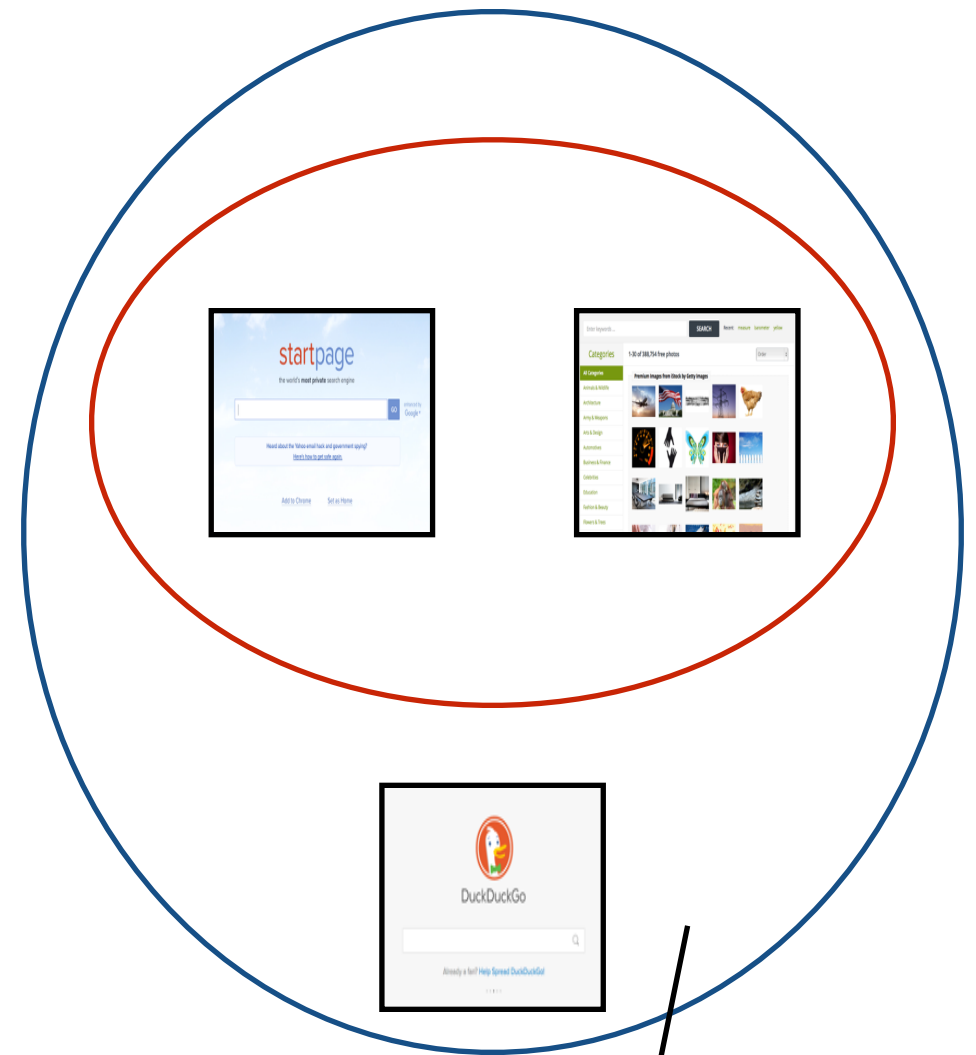
<b>Defence</b>	<b><math>(\epsilon, \Phi)</math>-privacy</b>	<b>Time OH</b>	<b>Packet OH</b>
<b>No Defence</b>	(0.05, k-NN)	0%	0%
<b>Decoy Pages</b>	(0.29, k-NN)	134%	59%
<b>BuFLO</b>	(0.29, k-FP)	110%	79%
<b>Tamaraw</b>	(0.25, k-NN)	258%	341%
<b>CS-BuFLO</b>	(0.16, k-FP)	67%	576%
<b>WTF-PAD</b>	(0.18, CUMUL)	247%	0%

# Q: What about priors?

- If true prior probabilities on web pages known, they can be used (i.e., bias the dataset accordingly).
- Ratio of success of one-try adversaries over random guessing maximized by uniform priors (Braun et al., 2009).



# Q: Open World?



Adversary knows



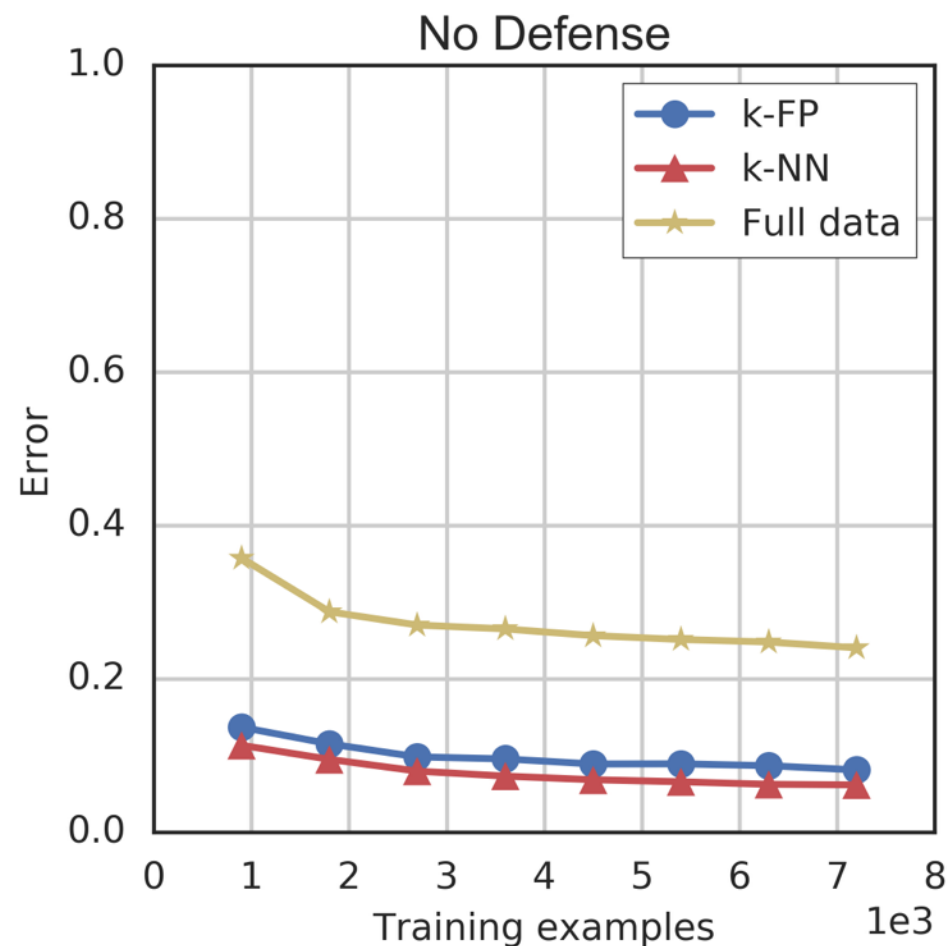
Victim may visit

y = "open"

# Q: Bounds on full info?

**Theorem** For any transformation  $\Phi: \mathcal{P} \rightarrow \mathcal{X}$ ,  
 $R^*(\mathcal{P}) \leq R^*(\Phi)$

However,



Q: Is the code available?

Yes

<https://github.com/gchers/wfes>

# Bayes, not Naïve

Security Bounds on Website Fingerprinting Defenses

Giovanni Cherubin

Privacy Enhancing Technologies Symposium

Minneapolis, Minnesota, USA

19 July, 2017

@gchers

